

The limit of a recurrence relation

Consider the recurrence relation

$$u_{n+1} = 0.6u_n + 8$$

We can determine this limit algebraically as follows.

Let L be the limit of the recurrence relation (1) above. Then

$$\begin{aligned}L &= 0.6L + 8 \\L - 0.6L &= 8 \\0.4L &= 8 \\L &= 8/0.4 \\&= 20\end{aligned}$$

In each example below - Obtain the limit algebraically.

1. $u_{n+1} = 0.8u_n + 5$
2. $u_{n+1} = 0.1u_n + 4$
3. $u_{n+1} = 0.5u_n + 8$
4. $u_{n+1} = -0.2u_n + 7$
5. $u_{n+1} = -0.75u_n + 2$
6. $u_{n+1} = 0.95u_n + 3$
7. $u_{n+1} = -0.6u_n + 2$
8. $u_{n+1} = 5 - 0.3u_n$
9. $u_{n+1} = 0.64u_n + 10$
10. $u_{n+1} = 0.82u_n + 6$