

# The limit of a recurrence relation

Consider the recurrence relation

$$u_{n+1} = 0.6u_n + 8$$

We can determine this limit algebraically as follows.

Let  $L$  be the limit of the recurrence relation (1) above. Then

$$\begin{aligned} L &= 0.6L + 8 \\ L - 0.6L &= 8 \\ 0.4L &= 8 \\ L &= 8/0.4 \\ &= 20 \end{aligned}$$

In each example below - Obtain the limit algebraically.

1.  $u_{n+1} = 0.8u_n + 5$

2.  $u_{n+1} = 0.1u_n + 4$

3.  $u_{n+1} = 0.5u_n + 8$

4.  $u_{n+1} = -0.2u_n + 7$

5.  $u_{n+1} = -0.75u_n + 2$

6.  $u_{n+1} = 0.95u_n + 3$

7.  $u_{n+1} = -0.6u_n + 2$

8.  $u_{n+1} = 5 - 0.3u_n$

9.  $u_{n+1} = 0.64u_n + 10$

10.  $u_{n+1} = 0.82u_n + 6$